

# COMBINED CLASSIFIERS FOR TIME SERIES SHAPELETS

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## ABSTRACT

*Time-series classification is widely used approach for classification. Recent development known as time-series shapelets, based on local patterns from the time-series, shows potential as highly predictive and accurate method for data mining. On the other hand, the slow training time remains an acute problem of this method. In recent years there was a significant improvement of training time performance, reducing the training time in several orders of magnitude. This work tries to maintain low training time- in the range from several second to several minutes for datasets from the popular UCR database, achieving accuracies up to 20% higher than the fastest known up to date method. The goal is achieved by training small 2,3-nodes decision trees and combining their decisions in pattern that uniquely identifies incoming time-series.*

## KEYWORDS

*Data mining, Time-series shapelets, Combining classifiers*

## 1. INTRODUCTION

The time-series shapelets classification method was introduced by Ye and Keogh [1] as a new type of data mining method, that uses the local features of time-series instead of their global. That makes it less sensitive to obstructive noise [1]. This method is successfully applied to a variety of application areas benefiting from its short classification time and high accuracy. Despite its advantages it has a significant disadvantage- a very slow training time. Current research mostly focuses on searching shapelets from all possible combination of time-series derived from a dataset [1, 2], keeping the training process relatively slow. A variety of proposals have been introduced to reduce the candidate shapelets [1, 2, 4, 5], but training time is still in the range of hours for some datasets. A newly introduced method [7] shrinks significantly the training time, making the training process to last from portion of a second to several seconds for investigated 45 datasets from UCR collection [9]. Although, this is the fastest up to date training method as of our knowledge, it also maintains high accuracies in compare with other state-of-arts methods [7]. In this paper we introduce a new method that reaches higher accuracies compared with the method from [7], keeping the training time in observable limits. We tested with 24 datasets from [9], the ones with number of classes higher than five. It was found that proposed method outperforms in terms of accuracy the method from [7] for most datasets. The achieved training time is kept low, varying from several seconds to several minutes, depending on a dataset. High accuracy and relatively short training time makes proposed method very competitive to present state-of-arts methods, which lack either accuracy or have huge training time.

The rest of this paper is organized as follows. In section 2 related work is presented. Section 3 describes the proposed method and gives technical details of its implementation. Section 4 discusses achieved results. Finally, section 5 summarizes the proposed method and gives ideas for further work.

## 2. RELATED WORK

Shapelet by definition is a sequence of samples that originate from one of the time-series from a dataset and maximally represent certain class. The classical method of shapelets discovery, known as *brute force algorithm* [1], employs all possible subsequences from all time-series from the train dataset and treat them as candidate shapelets. To test a candidate shapelet how well separates two classes A and B, all distances between the candidate shapelet and time-series from A and B are formed. These distances are ordered into a histogram and the histogram is consecutively split into two parts until the best information gain is achieved. The split point is named optimal split distance and distances below it considered to belong to class A, but above it to class B. If any other candidate shapelet achieves higher information gain, it is selected as shapelet. The process continue until all the candidate shapelets are processed. The method requires vast amount of calculation time. First improvements include *subsequence distance early abandon* of calculated distances and *admissive entropy pruning* based on predicted information gain [1]. These improvements reduced the total required time for training, but the reduction was not that significant [6]. Another idea based on the *infrequent shapelets*, prunes the non-frequent candidate shapelets [4]. More improvements [2] suggests using of so called *logical shapelets*, that reuse the computation and optimize the search space. Recent approach is based on synthesizing shapelets from random sequences, using *particle swarm optimization* techniques [6]. A new development in the area [7], vastly improves the training time of the shapelets by pruning candidate segments, which shows similarity in Euclidian distance space. This approach [7] is the fastest up to date as of our knowledge and in terms of accuracy is competitive with the current state-of-arts methods. We selected this method as a reference to proposed method, aiming to achieve similar or better accuracies, maintaining relatively low training time.

## 3. PROPOSED METHOD

Our previous research [6] changes the traditional way of producing shapelets by synthesizing a shapelet from randomly generated sequences using particle swarm optimization (PSO), instead of extracting the shapelets from the original time-series. It finds the shapelet for every pair of classes presented in a dataset, then combines them in a decision tree and find the decision tree that achieves highest accuracy. Producing the most accurate decision tree requires all possible combinations of trees to be tested. That is a slow process for more than four classes and adds additional processing time to traditionally slow training time. For this purpose, only datasets with less than five classes were investigated in [6]. Datasets with more than five classes are processed with the method introduced in this paper. The proposed method utilizes groups of small (up to 4 classes) decision trees, instead of building one big decision tree that contains all classes. When a time-series comes for classification every present tree produce a decision. The *decision path* taken during classification is present as string of characters. The decision paths from all present trees are combined into *decision pattern*. Every class from the datasets appears to maintain unique decision pattern. The patterns from training datasets are kept and when new time-series from test dataset comes for classification these patterns are compared with the pattern produced

from incoming time-series. The incoming time-series is associated with the class, to which its decision pattern mostly match.

### 3.1. Training

#### 3.1.1. Extracting subsets

The first step of the training process is to extract subsets of classes out of the original dataset, for which the decision trees will be defined. It is best to have uniform distribution of class indexes into subsets, as it allows non dominant class indexes into the final solution. The maximum amount of subsets  $L$  is defined as:

$$L = K! / (K - n)! n! \quad (1)$$

where,  $K$  is the number of all classes in a dataset and  $n$  is the number of classes in a subset  $n = 2, 3, 4$ .

In case the number of classes in the original dataset is relatively high (Fig.1,  $K = 37$ ), and the subsets consists of four classes for example, the final number of possible subsets combinations becomes  $66045$ , according (1). That is vast amount of subsets and training all of them will defeat the purpose of simplifying the calculations process. Instead of taking all possible combinations we can operate with just limited amount of subsets, obeying the rule of uniform distribution of class indexes as shown on Fig.1. Taking limited amount of subsets will not always fully obey the uniform rule. For example, on Fig.1 most of classes are present 3 times, but class 21, 29 and 30 are present just two times. Practically, it is enough all class indexes to be present into the subsets and the difference between the number of times classes are present to be no more than one.

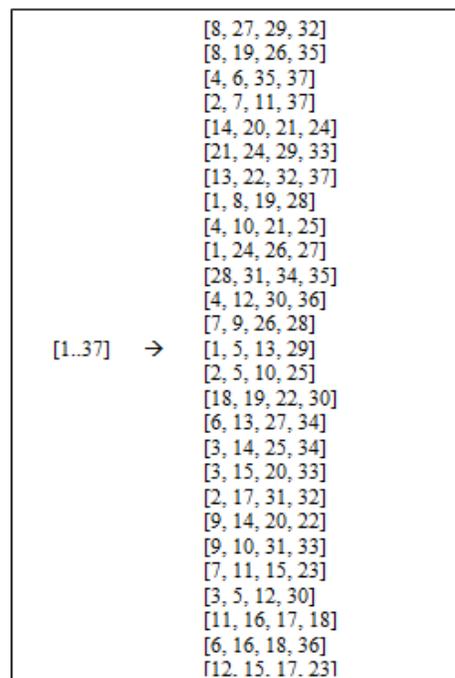


Fig. 1 Extracted subsets of 4-class combinations from a dataset with class indexes [1..37].

### 3.1.2. Training decision trees

Next step of the training process is to create decision trees for extracted subsets. Method from [6] is applied for these subsets as they consist of up to four classes. The method in [6] applies Particle Swarm Optimization (PSO) techniques, treating candidate shapelets as particles, which form a swarm. To find a shapelet between two classes A and B, swarm of  $N-2$  candidate shapelets is formed. The candidate shapelet represent a random sequence of samples and  $N$  is the length of the time-series in a dataset. Every such sequence has different length, varying from 3 (the smallest meaningful shapelet length) up to  $N$ . These potential candidates cover the whole range of possible shapelets lengths. These candidate shapelets compete to each other to find the best solution- a sequence that maximally separates two classes A and B. On every step of the process the candidate shapelet changes its values according to the best overall values in the swarm and candidates best values so far. The fitness function applies functionality similar to the criterions of the brute force algorithm. After calculating the distances between the candidate shapelet and time-series from class A and class B, it builds a histogram of distances and calculate the possible highest information gain. If currently calculated information gain is bigger than information gain assigned so far to the candidate, current values becomes particle's best values. If currently calculated information gain is bigger than information gain of the best candidate shapelet, then current candidate shapelet become the best candidate of overall swarm. Iteration stops when pre-defined number of iterations is achieved or when best information gain from iteration to iteration remains the same.

Described particle searching process is relatively fast, but high number of candidate shapelets may slow down the training process in general. For that, two improvements were introduced. First, compression of the training data is introduced, which according to [7] will not harm the training process, but improves the performance. Second, we introduce the idea that not  $N-2$  candidate shapelets are required, but only 10 will be enough to compete and find the best shapelet among them. As candidate shapelets have different lengths it is important to know which of them to remove from the competition. To find the ten most representative shapelets lengths, we extract from the training dataset only a few time-series per class and train with them. In this partial training process we use  $N-2$  shapelets candidates. The partial training is very fast as just few time-series were used, but it shows well which are the most popular shapelets lengths for certain subset. Based on these results, we select the 10 most popular shapelets lengths and run the process again.

When all pair of classes in a subset have their shapelets discovered, then all possible variations of decision trees for this subsets are checked and the one that produces the highest accuracy is selected. The accuracy of the decision trees during the training process is checked with time-series from the training dataset.

### 3.1.3. Decision patterns

An important term in proposed method is the *decision path*. The decision path is the path taken through the decision tree during decision process. When time-series comes for classification, the distance between shapelet and the time-series is calculated. If such distance is higher than the optimal split distance associated with the shapelet, the process takes the right branch of the tree, if not- the process takes the left branch. When right branch is taken, character "R" is added to the decision path, when the left branch is taken, character "L" is added to the decision path. The path

length is equal to the tree depth. An example of possible decision paths are shown on Fig.2. To form a *decision pattern* the decision paths from all decision trees are concatenated as shown on Fig. 3. For example, if the system consists of 6 decision trees and every tree has two nodes similar to that on Fig.2, then one possible variant of decision patterns is {RL,RR,R-,L-LL,RL}. During the training process, decision pattern for every time-series from the training dataset is collected. These decision patterns are kept and used during the classification process. Keeping the decision patterns into memory requires certain amount of memory to be allocated during the classification process. For example, “*Non.FatalECG.1*”[9] dataset contains 1800 train time-series and the chosen pattern length is 836 characters. If we consider that a character is encoded with 1 byte then required memory during classification process is in the vicinity of 1.5MB. That is feasible amount for the modern computers, but may cause difficulties in small embedded systems. The direction (“R/L/-”) of the decision path currently requires 1 bytes (8 bits) of encoding, but it could be optimized to two bits to reduce the required amount of memory, especially in the embedded systems.

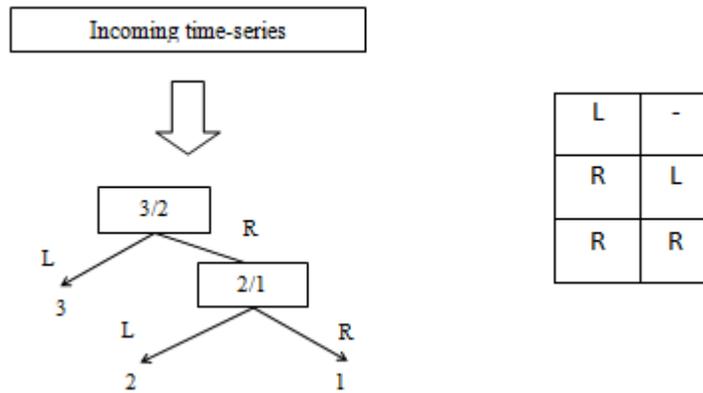


Fig.2 Possible decision paths of the illustrated decision tree obtained after classification of incoming time-series

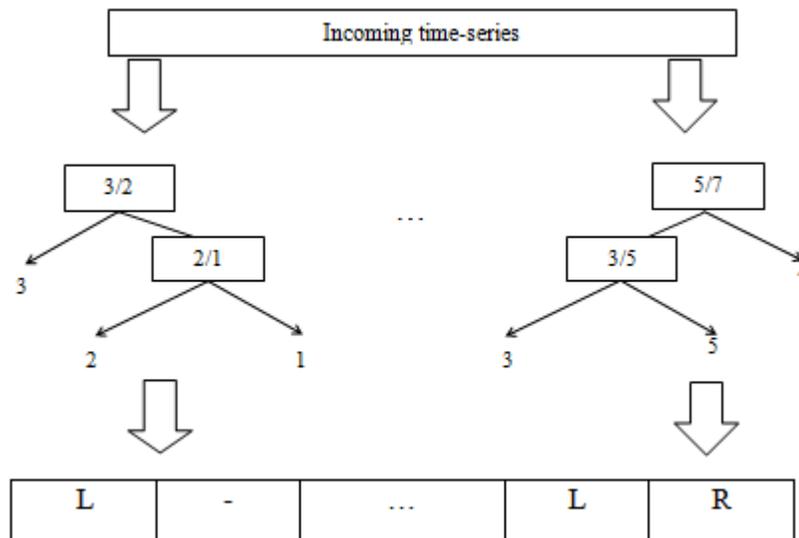


Fig.3 Decision pattern, obtained by combining the decision paths from all subsets' decision trees.

### 3.2. Classification

When time-series from test dataset comes for classification a decision pattern is created for that time-series. This pattern is compared with the patterns produced during the training process. Comparison process is very simple. The two decision patterns strings are compared character by character in place and the comparison coefficients is equal to the number of characters that coincide by place and value, divided by the length of the decision string as shown on Fig. 4. After all the comparison coefficients are collected we keep only those which are above certain threshold of  $0.98$ . The idea of this classification is that time-series from the same class will produce similar decision patterns, but decision patterns from different classes will differ a lot. The incoming time-series is identified as class to which it has closest decision pattern. In certain cases more than one class index show similar pattern to the investigates time-series. In such cases the classification process assign the incoming time-series to the class, that has majority of decision patterns closest to the incoming time-series decision pattern.

R	-	L	L	R	-	L	L	L	R
R	L	L	L	L	-	L	R	L	L

Fig. 4 Comparison between decision patterns of two time-series. Six out of ten characters coincide by place and value, therefore the comparison coefficients is  $6/10 = 0.6$ .

## 4. EXPERIMENTAL RESULTS

The project implementation uses C# and .NET Framework 4.0. Time performance measurements were produced with a *System.Diagnostics.StopWatch* .NET class. In our experiments we used a PC with the following parameters: CPU: Intel Core i7, 2.4GHz; RAM: 8 GB; 64-bit Windows 7 OS. We selected datasets from the UCR collection [9] with a number of classes higher than five (Table 1) as for datasets with fewer classes applying proposed method is meaningless. Table 1 shows parameters of the used datasets. We used method from [7] as a reference method. It produces the fastest training time as of our knowledge and accuracies that outperform most of state-of-arts method for the moment. We downloaded the Java implementation of the proposed method from [10] and ran it on the same hardware as proposed method. Reference method requires to specify threshold  $p$  and aggregation ratio  $r$ . We kept these value the same as in [7] to maintain the highest accuracy. Table 3 shows the results of both methods in terms of training time and accuracies they produce. In 18 out of 24 cases the proposed method outperforms the reference method in terms of accuracy, where the improvements vary from 2% up to 23%, where in six of these cases the improvement is above 10%. In the rest, 3 cases differ less than 1.0% and we consider that both method perform equally in this cases. Only in 3 cases the reference method outperform the proposed method in terms of accuracy, but the difference is less than 2%. Although the reference method shows better training times, the proposed method maintains an observable training time- varying from several seconds up to several minutes (~15 min. for Non.FatalECG.1) for datasets that have long time-series and higher number of time-series in a train datasets (uWave.X, uWave.Y, uWave.Z).

Proposed method uses the decision patterns from all time-series in the training datasets thus, in some cases the classification process may slow done due to high number of time-series in the train dataset (Non.FatalECG.1, Non.FatalECG.2). In some cases the length of the decision pattern

could be relatively long (Adiac- 1473, Non.FatalECG.1- 836) which may also influence the classification time. To investigate this issue we have measured the averaged classification time per time-series. Table 2 represents the results. In the most heavy case (Non.FatalECG.1) when the number time-series is 1800 and the decision pattern string length is 836 characters the classification time is above 200 milliseconds. The length of the decision pattern may vary as shown on Table 3. For datasets, such as “Beef”, which consist of 5 classes, the number of subsets is limited to 10 when constructed of 3 class indexes or to 5 when constructed of 4 class indexes. In this case to achieve better accuracy, combination of all possible trees up to 4 indexes are taken. On the other hand, datasets with more class indexes have more varieties to choose from. In the case of “50Word” dataset, which contain 50 class indexes, the total amount for combinations for two-classes decision tree is 1225. We selected 497 of them based on the principle from 3.1.1 and the total length of the decision pattern become 994 characters. Rising the number of characters in the decision pattern in all investigated cases increased the accuracy in general. Although, it appears that there is certain limit of characters above which the accuracy does not increase and even may decrease as shown on Table 4.

Table 1. Used datasets from UCR database.

Dataset	Number of Classes	Number of time-series in the train/test dataset	Time-series length
Beef	5	30 / 30	470
Haptics	5	155 / 308	1092
OsuLeaf	6	200 / 242	427
Symbols	6	25 / 995	398
synthetic.	6	300 / 300	60
Fish	7	175 / 175	463
InlineSkate	7	100 / 550	1882
Lighting7	7	70 / 73	319
MALLAT	8	55 / 2345	1024
uWave.X	8	896 / 3582	315
uWave.Y	8	896 / 3582	315
uWave.Z	8	896 / 3582	315
MedicalImages	10	381 / 760	99
Cricket X	12	390 / 390	300
Cricket Y	12	390 / 390	300
Cricket Z	12	390 / 390	300
FaceAll	14	560 / 1690	131
FacesUCR	14	200 / 2050	131
SwedishLeaf	15	500 / 625	128
WordsS.	25	267 / 638	270
Adiac	37	390 / 391	176
Non.FatalECG.1	42	1800 / 1965	750
Non.FatalECG.2	42	1800 / 1965	750
50words	50	450 / 455	270

Table 2. Averaged classification times produced by proposed method.

Dataset	Classification Time, [msec]	Dataset	Classification Time, [msec]
Beef	0.38	MedicalImages	4.27
Haptics	1.05	Cricket X	11.48
OsuLeaf	1.67	Cricket Y	9.07
Symbols	0.72	Cricket Z	9.07
synthetic.	1.81	FaceAll	10.06
Fish	3.97	FacesUCR	3.97
InlineSkate	4.14	SwedishLeaf	16.03
Lighting7	2.17	WordsS.	17.75
MALLAT	2.11	Adiac	64.56
uWave.X	3.98	Non.FatalECG.1	223.52
uWave.Y	5.87	Non.FatalECG.2	195.99
uWave.Z	3.84	50words	66.77

Table 3. Experimental results presenting accuracies and training times of the proposed and reference method.

Dataset	Comp. Rate	Proposed method			Reference method	
		Pattern Length	Train Time, [sec]	Accuracy, [%]	Train Time, [sec]	Accuracy, [%]
Beef	0.125	70	4.15	<b>52.21</b>	0.05	48.89
Haptics	0.500	20	70.66	<b>39.39</b>	1.69	34.56
OsuLeaf	0.125	150	55.84	<b>76.99</b>	0.14	53.31
Symbols	0.250	150	7.87	<b>94.20</b>	0.05	82.48
synthetic.	0.250	150	125.58	98.88	0.06	98.44
Fish	0.250	287	102.51	<b>90.85</b>	0.15	75.05
InlineSkate	0.125	245	78.57	39.57	0.56	39.88
Lighting7	0.500	245	42.52	<b>75.79</b>	0.39	65.30
MALLAT	0.125	280	42.87	<b>92.85</b>	0.10	90.77
uWave.X	0.250	117	559.22	75.32	4.37	<b>76.45</b>
uWave.Y	0.250	168	594.66	65.12	3.33	<b>66.72</b>
uWave.Z	0.125	117	508.93	66.30	1.89	<b>67.48</b>
Med.Images	0.500	240	139.47	<b>71.27</b>	0.58	67.68
Cricket X	0.250	471	267.66	<b>77.78</b>	0.61	68.63
Cricket Y	0.250	408	198.58	<b>79.14</b>	0.50	64.01
Cricket Z	0.250	414	184.38	<b>75.29</b>	0.66	68.21
FaceAll	0.500	342	167.02	<b>75.42</b>	1.25	71.63
FacesUCR	0.500	330	36.97	<b>90.56</b>	0.32	84.61
SwedishLeaf	0.500	519	342.27	<b>91.14</b>	0.34	85.60
WordsS.	0.250	600	28.48	<b>65.46</b>	0.29	60.92

Adiac	0.500	1473	514.63	<b>73.65</b>	0.27	55.67
Non.FatalECG.1	0.250	836	878.18	<b>85.01</b>	6.90	80.93
Non.FatalECG.2	0.125	836	349.32	<b>89.19</b>	4.67	86.34
50words	0.250	994	58.15	68.79	0.35	68.06

Table 4. Accuracy dependency from decision pattern length for “Lighting7”( 7 classes) dataset.

Decision Pattern Length (number of trees x number of classes in tree )	Training Time, [sec]	Accuracy, [%]
21x2	4.09	61.64
35x3	16.28	71.23
35x4	30.90	71.68
35x4 + 35x3	42.52	<b>75.79</b>
35x4 + 35x3 + 21x2	44.29	73.97

## 5. CONCLUSION AND FUTURE WORK

This paper proposes a new method for time-series shapelets classification, which demonstrate higher accuracies than produced by fastest known state-of-arts method for most of the investigated cases. As well it keeps an observable time for training, varying from several seconds to several minutes.

As future work we will focus on improving the training time even further, applying parallel processing based calculations (utilizing *.NET Parallel.ForEach*) that employ all possible processor’s cores on certain machine. This technology could be successfully applied on variety of places in proposed method where the calculations from current stage are independent from each other, namely: iteration steps of the PSO algorithm for shapelets discovery; the comparison between incoming time-series pattern and available decision patterns.

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