

OPTIMAL SIZING AND PLACEMENT OF DISTRIBUTED GENERATORS AND CAPACITORS IN RADIAL DISTRIBUTION NETWORK

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ABSTRACT

Distribution network is an integral part of power system and it acts as the interface with consumer load points. The network incurs significant amount of losses in the electrical system. Loss minimization remains one of the prime objectives in distribution network optimization. This paper proposes an application of L-SHADE algorithm to simultaneously size and place both distributed generators (DGs) and shunt capacitors (SCs) in distribution network to reduce system real power loss. SHADE is the success history based parameter adaptation technique of differential evolution (DE). L-SHADE improves the performance of SHADE by linearly reducing the population size in successive generations. The algorithm is applied to minimize loss in standard IEEE 33-bus radial distribution network (RDN) and the simulation results are compared with some recent studies on the topic.

KEYWORDS

Radial distribution network, Distributed generator (DG), Shunt capacitor (SC), Power loss, L-SHADE algorithm

1. INTRODUCTION

Mitigating ever increasing load demand is one of the major challenges faced by utility companies. It may not always be feasible to boost capacity of transmission network. Locally installed distributed generators (DG) and added shunt capacitor (SC) banks in the system can augment the capacity, reduce losses, improve voltage profile and power quality of the network. Distributed generators can be a diesel generator, a wind turbine, solar photovoltaics (PV), fuel cells etc. Optimal sizing and siting of both distributed generators and shunt capacitors are of significance in improving system performance. Several literatures [1-3] focused on optimal sizing and placement of DGs only in pursuit of real power loss minimization. A network comprising both DG and SC has been studied in few literatures. Naik et al. [4] took analytical approach to optimally size and locate both the components. In most recent papers, heuristic methods such as hybrid harmony search algorithm (HSA) and particle artificial bee colony (PABC) [5], intersect mutation differential evolution (IMDE) [6] and back-tracking search algorithm (BSA) [7] have been applied for optimal design of capacity and placement of both distributed generators and shunt

capacitors. Ref. [8] optimizes size and location of both DG and SC in various networks with simultaneous minimization of both real and reactive power losses using decomposition based multi-objective evolutionary algorithm (MOEA/D).

The current study implements L-SHADE [9] algorithm to optimally locate and size both DG and SC in radial distribution network. SHADE [10] is a success history based parameter adaptation technique of DE optimization process for a constrained, multimodal non-linear problem. The convergence of the algorithm to global optima is fast and it potentially outperforms most other DE variants on CEC benchmark problems [9]. SHADE exhibited good performance in optimal power flow solutions [11]. In recent times L-SHADE has successfully been applied and has shown very competitive performance in windfarm layout optimization [12], in total harmonic distortion minimization of multilevel inverters [13], in hybrid active power filter parameter optimization [14] etc. Motivated by the growing application and noteworthy performance of L-SHADE in power domain, we apply the algorithm on the problem of radial distribution network (RDN). The distribution network is to be reinforced with optimally sized and appropriately placed DGs and SCs so that network real power loss is minimized. As an obvious fact, the problem is about simultaneous optimization of discrete variables i.e. locations (bus nos.) of all the components and continuous variables i.e. ratings of all the components. Further, the problem is non-linear due to the requirement of power flow calculation that involves numerous system components.

The organization of rest of the paper is done following way. Section 2 includes the mathematical formulation of power flow in distribution network. Section 3 describes the algorithm and its application. Section 4 discusses the case studies and simulation results. The paper ends with conclusion and possible future work in section 5.

2. MATHEMATICAL MODEL

The mathematical formula pertaining to power flow in the network are presented in this section with the aid of a simple feeder configuration.

2.1. Power flow formulation

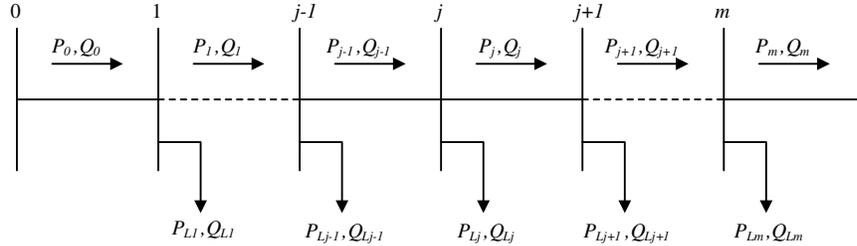


Fig. 1. Single line diagram of a radial feeder [8]

Single line diagram of a simple feeder-line configuration is shown in Fig. 1. The computation of power flow is performed by following equations [8]:

$$P_{j+1} = P_j - P_{Lj+1} - R_{j,j+1} \cdot \frac{P_j^2 + Q_j^2}{|V_j|^2} \quad (1)$$

$$Q_{j+1} = Q_j - Q_{Lj+1} - X_{j,j+1} \cdot \frac{P_j^2 + Q_j^2}{|V_j|^2} \quad (2)$$

$$\begin{aligned} |V_{j+1}|^2 = |V_j|^2 - 2(R_{j,j+1} \cdot P_j + X_{j,j+1} \cdot Q_j) \\ + (R_{j,j+1}^2 + X_{j,j+1}^2) \cdot \frac{P_j^2 + Q_j^2}{|V_j|^2} \end{aligned} \quad (3)$$

where, real power and reactive power flowing out of bus j are P_j and Q_j respectively; P_{Lj+1} and Q_{Lj+1} are the real load and reactive load connected at bus $j + 1$. Line section between buses j and $j + 1$ has resistance $R_{j,j+1}$ and reactance $X_{j,j+1}$. $|V_j|$ is the voltage magnitude of bus j . The power loss in line segment connecting buses j and $j + 1$ is computed using following equation:

$$P_{Loss}(j, j + 1) = R_{j,j+1} \cdot \frac{P_j^2 + Q_j^2}{|V_j|^2} \quad (4)$$

where, real power loss is defined by P_{Loss} . Total real power loss, the optimization objective in the network, is obtained by summing up all the line losses as follows:

$$TP_{Loss} = \sum_{j=0}^{m-1} P_{Loss}(j, j + 1) \quad (5)$$

In this study, we consider DG units supplying real power with unity power factor e.g. photovoltaic systems, micro turbines etc. Therefore, if a DG, delivering power output of P_{DG} , is added to a bus (say j -th bus), the load in that bus changes from P_{Lj} to $(P_{Lj} - P_{DG})$. Similarly, if k -th bus in the system has inductive load of Q_k , an addition of Q_C unit of capacitor bank alters the reactive load to $(Q_k - Q_C)$. During the search process, the algorithm checks all possible locations with all probable ratings of the equipment to decide best combination that results in minimum power loss.

2.2. Constraints

Magnitude of any bus voltage must lie within specified limits of maximum and minimum voltages. Current in any branch shall not exceed the rated capacity of the branch. Mathematically, these can be written as:

$$V_{min} \leq |V_j| \leq V_{max} \quad (6)$$

$$|I_{j,j+1}| \leq I_{j,j+1(max)} \quad (7)$$

where, V_{max} and V_{min} are the maximum and minimum allowable voltages for any bus in the network. The numerical values of these parameters for the systems are considered as 0.90 p.u. and 1.05 p.u. respectively. $|I_{j,j+1}|$ is the magnitude of current flowing in the line linking bus j and bus $j + 1$, while $I_{j,j+1(max)}$ is the maximum permissible current through the same branch considering the thermal capability limit of the line. It is worthwhile to mention that current carrying capacities of the branches in IEEE bus system are not explicit. Moreover, as installation of DGs and SCs improve the voltage profile of the network, the current reduces from the base configuration. Hence, verification of this constraint is not necessary.

3. L-SHADE ALGORITHM AND APPLICATION

Differential Evolution (DE) is a stochastic, population based optimization algorithm [15]. SHADE [10] is success history based adaptive DE where control parameters scaling factor (F) and crossover rate (CR) are automatically adjusted during the evolution process. Algorithm L-SHADE [9] is an extension of SHADE. In L-SHADE, the population size is dynamic and it reduces in successive generations following a linear function. The algorithm alongwith its application on RDN problem is briefly described in this section.

3.1. Initialization

Firstly, DE optimization process creates an initial population of probable solutions by assigning random values (within feasible bound) to each decision vector of the population. Initialization of j -th component of i -th decision vector is done as [16]:

$$x_{i,j}^{(0)} = x_{min,j} + rand_{ij}[0,1] * (x_{max,j} - x_{min,j}) \quad (8)$$

where $rand_{ij}[0,1]$ is a random number lying between 0 and 1. The superscript '0' signifies initialization of population members.

3.2. Mutation

In next step during mutation process, donor/mutant vector $v_i^{(t)}$ is created corresponding to each population member or target vector $x_i^{(t)}$ in the current generation t . The mutation strategy used here is 'current-to- p best/1':

$$v_i^{(t)} = x_i^{(t)} + F_i^{(t)} \cdot (x_{pbest}^{(t)} - x_i^{(t)}) + F_i^{(t)} \cdot (x_{R_1}^{(t)} - x_{R_2}^{(t)}) \quad (9)$$

The mutually exclusive integers R_1^i & R_2^i are randomly chosen from the population range $[1, Np]$; $x_{pbest}^{(t)}$ is randomly selected from top $100p\%$ ($p \in [0,1]$) individuals of current generation. The positive control parameter $F_i^{(t)}$ scales the difference vectors at t -th generation. The mutation strategy adopted in L-SHADE helps to exploit the search space efficiently and converge into an optimal solution.

3.3. Parameter adaptation

At each generation t , each individual has its own $F_i^{(t)}$ and $CR_i^{(t)}$ parameters that are used to generate the trial vector. Adaptation of these two parameters follows as:

$$F_i^{(t)} = randc(\mu F_r^{(t)}, 0.1) \quad (10)$$

$$CR_i^{(t)} = randn(\mu CR_r^{(t)}, 0.1) \quad (11)$$

where $randn(\mu CR_r^{(t)}, 0.1)$ and $randc(\mu F_r^{(t)}, 0.1)$ are the sampled values from Normal and Cauchy distributions respectively. Normal distribution has a mean of $\mu CR_r^{(t)}$ and a variance of 0.1. Location and scale parameters of Cauchy distribution are $\mu F_r^{(t)}$ and 0.1 respectively. $\mu F_r^{(t)}$ & $\mu CR_r^{(t)}$ are randomly chosen from successful candidates of past generations saved in a

memory. The two values are initialized to 0.5 and subsequently modified by weighted Lehmer mean [9,10].

3.4. Crossover

Donor vector $v_i^{(t)}$ enters into the trial/offspring vector $u_i^{(t)} = (u_{i,1}^{(t)}, u_{i,2}^{(t)}, \dots, u_{i,d}^{(t)})$ by mixing its components with target vector $x_i^{(t)}$ through crossover. Binomial crossover is most commonly employed and it operates on each element based on adapted crossover rate $CR_i^{(t)}$. The scheme for an element is defined as:

$$u_{i,j}^{(t)} = \begin{cases} v_{i,j}^{(t)} & \text{if } j = j_{rand} \text{ or } rand_{i,j}[0,1] \leq CR_i^{(t)}, \\ x_{i,j}^{(t)} & \text{otherwise} \end{cases} \quad (12)$$

where j_{rand} is a randomly chosen natural number in $\{1, 2, \dots, d\}$, and d is the dimension of the decision vector.

3.5. Linear population size reduction

The success of SHADE algorithm is attributed to the adaptation technique of scale factor F and crossover rate CR . It has also been found that dynamic reduction in population size improves performance of SHADE. L-SHADE precisely implements the task by introducing a linear function for reduction of population size in successive generations. The population size starts with Np_{ini} (initial population size) and reduces closely matching the linear function before finally ending with Np_{min} (minimum population size). After each generation t , the population size in subsequent generation $t + 1$ is calculated by –

$$Np(t + 1) = \text{round} \left[\left(\frac{Np_{min} - Np_{ini}}{NFE_{max}} \right) \cdot NFE + Np_{ini} \right] \quad (13)$$

Np_{min} is set to 4 because mutation strategy adopted here requires minimum 4 individuals. NFE_{max} is the maximum number of fitness evaluations and NFE is the current number of fitness evaluations. If $Np(t + 1) < Np(t)$, worst ranking individuals totalling $[Np(t) - Np(t + 1)]$ are removed from the population [9]. A summary of steps involved in the optimization process is provided herein.

A. Input and initialization:

1. Input $Np_{ini} = 100$, $NFE_{max} = 20000$.
2. Define vector $x = [position, rating]$ and range of all these elements. We have 2 DG and 2 SC to size and allocate. So, a maximum of 4 elements for *position* (bus no.) and 4 elements for *rating* will form vector x (maximum, $d = 8$). Elements of position will always be rounded off to nearest integer.
3. Create random initial population of 100 such vectors defined as x_i as per equation (8), $i = 1, 2, \dots, 100$.
4. Set generation counter $t = 0$, dynamic population size $Np(t) = Np_{ini}$, evaluation counter $NFE = 1$ and control parameters $\mu F_r^{(0)} = \mu CR_r^{(0)} = 0.5$.

B. Algorithm loop:

1. Evaluate $f(x_i^{(t)})$ i.e. ' TP_{Loss} ' in equation (5) for $x_i^{(t)}$ where $i = 1$ to Np . Increase counter NFE by Np i.e. $NFE = NFE + Np$.
2. **while** termination criteria $NFE < NFE_{max}$ **do**
3. **for** $i = 1$ to Np **do**

4. Adapt control parameters $F_i^{(t)}$ and $CR_i^{(t)}$ as per equations (10) & (11).
5. Perform mutation to generate vector $v_i^{(t)}$ as per equation (9).
6. Perform crossover to generate element $u_{i,j}^{(t)}$ as per equation (12).
7. Evaluate $f(u_i^{(t)})$ i.e. ' TP_{Loss} ' for $u_i^{(t)}$. Increase evaluation counter NFE by 1 i.e. $NFE = NFE + 1$.
8. Select best fit individuals for next generation. If, $f(u_i^{(t)}) \leq f(x_i^{(t)})$ and constraints in eq. (6) & (7) are satisfied, $x_i^{(t+1)} = u_i^{(t)}$. Else $x_i^{(t+1)} = x_i^{(t)}$.
- End for** loop.

9. Update population size for next generation $Np(t + 1)$ as per LPSR strategy in equation (13).
10. Increase generation counter $t = t + 1$. Go to step 2 of algorithm loop.

4. CASE STUDY RESULTS AND COMPARISON

IEEE 33-bus standard radial distribution network (RDN) diagram is provided in Fig. 2. Total load of the network is 3.72 MW and 2.3 MVar. The maximum cumulative capacities of DGs (unity power factor) and capacitor banks in the installation are not to exceed 2 MW and 2 MVar respectively. Table 1 summarizes the case description, results and comparison. 3 case studies are performed for the RDN. Case-1 deals with addition of only DGs in the network. Case-2 is study of the RDN when only SCs are added, while Case-3 considers both DGs and SCs. Average runtime in normal PC for most complex Case-3 is about 90 seconds for one complete run of the algorithm (i.e. $NFE_{max} = 20000$ function evaluations) on MATLAB platform. As can be seen from the tabulated results, increasing number of DG and SC reduces the system loss drastically. However, as in [6], we consider maximum 2 nos. of DG and 2 nos. of SCs that can be connected to the network. The loss data given by L-SHADE algorithm for all cases are the lowest. In Case-1, bus location and equipment ratings proposed by L-SHADE, IMDE and BSA are quite similar. However, bus-13 for allocation of one DG is preferred to bus-14 for effectiveness in loss reduction. In Case-2, cumulative ratings of SCs suggested by both IMDE and L-SHADE are almost equal. Again, bus-12 is advantageous location for one SC rather than bus-14. Ratings proposed by L-SHADE for SCs are higher in Case-3 when compared with IMDE algorithm. However, resulting network loss, the prime objective of optimization, is much reduced with little reshuffle in placement of both DG and SC.

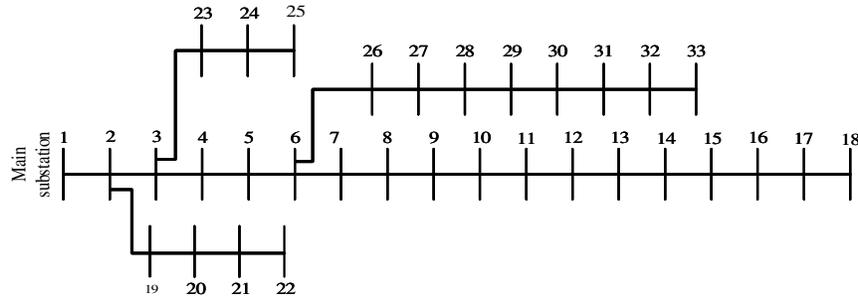


Fig. 2: Standard IEEE-33 bus test system

Table 1. Simulation results for IEEE 33-bus radial distribution network

Case description	Parameter	Various optimization methods				
		L-SHADE	IMDE [6]	Analytical [4]	Hybrid [5]	BSA [7]
Case-1 (DG only)	Real power loss, kW	85.91	86.12 ¹	142.34	111.03	87.16
	DG size, kW (bus no.)	1155 (30)	840 (14), 1130 (30)	1000 (18)	2598 (6)	851.6 (13), 1157.6 (30)
	Min bus voltage in p.u. (bus no.)	0.9685 (33)	0.9675 ¹ (33)	0.9311 (33)	0.9425 (18)	not reported
Case-2 (SC only)	Real power loss, kW	135.75	139.7	164.6		-
	SC size, kVAr (bus no.)	1039 (30)	467 (12), 1037 (30)	1000 (33)		-
	Min bus voltage in p.u. (bus no.)	0.9360 (18)	0.942 (18)	0.9165 (18)		-
Case-3 (DG + SC)	Real power loss, kW	28.50	32.08	84.28	58.45	30.87
	DG size, kW (bus no.)	1121 (30)	829 (13), 1080 (10), 896.4 (31)	447 (18), 559 (17)	2531 (6)	860 (13), 1310.5 (30)
	SC size, kVAr (bus no.)	1041 (30)	452 (12), 254.8 (16), 932.3 (30)	400 (33), 500 (32)	1250 (30)	334.8 (14), 899.8 (30)
	Min bus voltage in p.u. (bus no.)	0.9803 (25)	0.979 (25)	0.961 (30)	0.9536 (18)	not reported

¹ Values are recalculated with the proposed ratings of DG and SC [6]

Fig. 3 shows convergence of L-SHADE for Case-3. As observed from the diagram, the algorithm converges in less than 8000 fitness evaluations. Linear population size reduction technique is demonstrated in Fig. 4 where the population size reduces almost linearly to 4 individuals. Fig. 5 indicates bus voltage profiles for various case studies performed in this literature. Voltages of all buses are within the allowable limits. Further, more uniform voltage profile is obtained when multiple components with smaller ratings are distributed throughout the network.

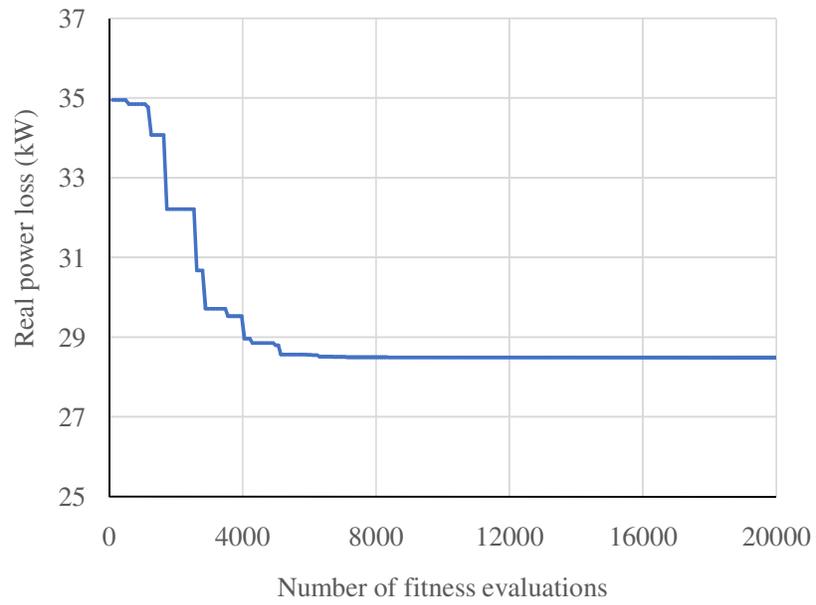


Fig. 3: Convergence of L-SHADE algorithm for Case-3

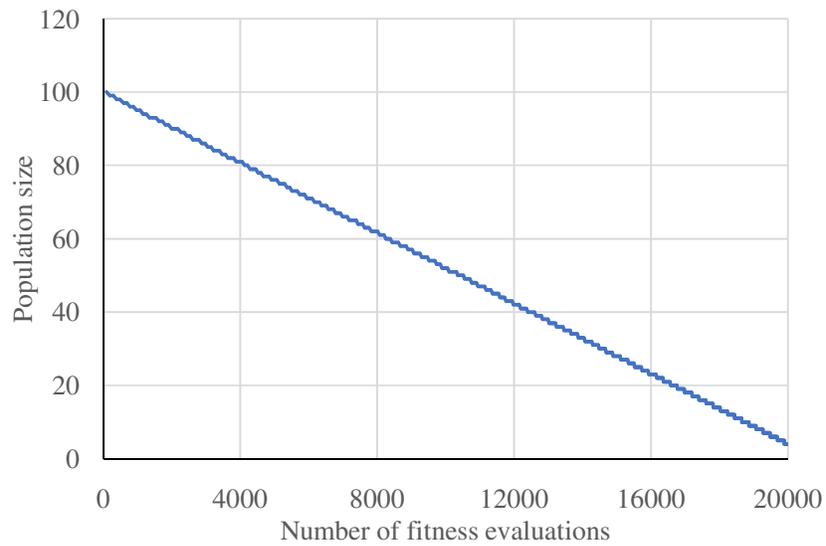


Fig. 4: Linear population size reduction of L-SHADE algorithm for Case-3

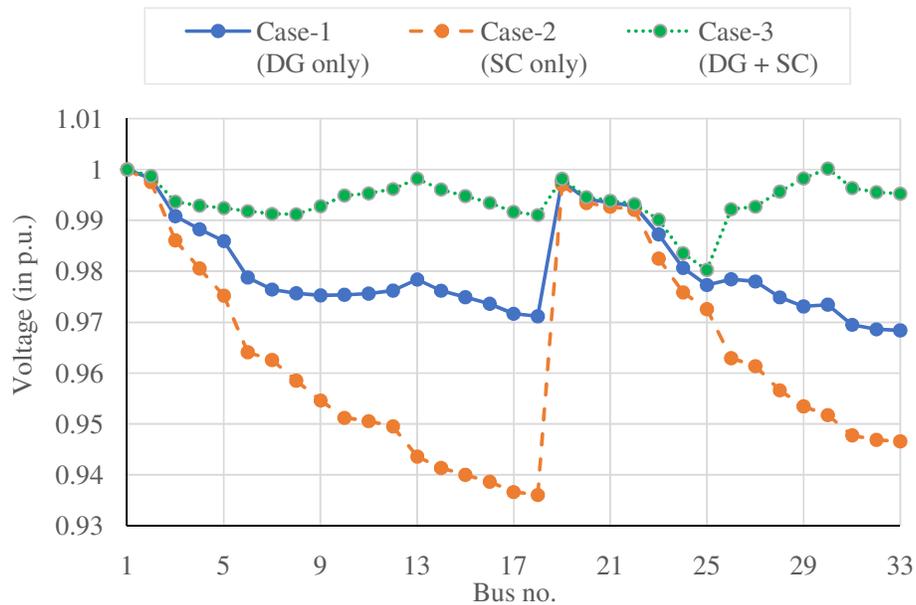


Fig. 5: Bus voltage profile of 33-bus system for various case studies

5. CONCLUSION

The present paper discusses in detail the application and usefulness of L-SHADE optimization algorithm for deciding the rating and location of DG and SC simultaneously in the distribution network to reduce real (active) power loss. Size and location proposed by the algorithm for the equipment lead to lower system real power loss than the loss achieved by other equivalent algorithms. Reduction of loss by any amount is of technical and commercial advantage. Further the algorithm converges to the optimal solution very fast. The effectiveness of the algorithm in reducing loss in the networks with large number of buses remains the topic for future study.

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